



- (a) Find the distribution of  $Y_i = \ln(2X_i - X_i^2)$ .
- (b) Find the maximum likelihood estimator (MLE) for  $\theta$ . Show that it is an asymptotically unbiased estimator for  $\theta$ .
- (c) Find the uniformly minimum variance unbiased estimator (UMVUE) for  $\theta$ .
- (d) Is the UMVUE an efficient estimator of  $\theta$ ?