Program in Applied Mathematics PROBABILITY AND STATISTICS PRELIMINARY EXAMINATION January 2014

Notice:Do four of the followingve problems. Place an X on the line1.opposite the number of the problem that you are NOT submitting2._____for grading.Please do not write your name anywhere on this exam.3._____You will be identified only by your student number, given below and4.______on each page submitted for grading.Show all relevant work.5.______Total__________________

Student Number _____

- 1. Consider *U* Uniform(0;1) and let *R* be a continuous random variable with probability density function $f(r) = re^{r^2 2}$, for r > 0. De ne:
 - $X := a + b R\cos(2 U)$ $Y := c + d R\sin(2 U)$

where

3. Consider i.i.d. random variables X_1 ; ...; X_n generated from the *Maxwell density*:

$$f(x) = \frac{5}{2} \frac{1}{2} \frac{x^2}{3} e^{-\frac{1}{2} \frac{x^2}{2}}; \qquad x > 0; \quad > 0:$$

Note this family satis es the \nice" regularity properties that are useful for examining maximum likelihood estimators. This density describes the distribution of speeds of molecules in thermal equilibrium.